NØthing is Logical

Maria Aloni ILLC & Philosophy University of Amsterdam M.D.Aloni@uva.nl Slides: https://www.marialoni.org/resources/WoLLIC24.pdf

WoLLIC 2024 Bern, 10 June 2024

NØthing is logical (Nihil)

- Goal of the project: a formal account of a class of natural language inferences which deviate from classical logic
- Common assumption: these deviations are not logical mistakes, but consequence of pragmatic enrichment
- Strategy: develop *logics of conversation* which model next to literal meanings also pragmatic factors and the additional inferences which arise from their interaction
- Novel hypothesis: neglect-zero tendency as crucial pragmatic/cognitive factor
- Main conclusion: deviations from classical logic consequence of pragmatic enrichments albeit not of the canonical Gricean kind



Non-classical inferences

Free choice (FC)

- (1) $\diamondsuit(\alpha \lor \beta) \rightsquigarrow \diamondsuit \alpha \land \diamondsuit \beta$
- (2) Deontic FC inference
 - a. You may go to the beach or to the cinema.
 - b. \rightsquigarrow You may go to the beach and you may go to the cinema.

(3) Epistemic FC inference

- a. Mr. X might be in Victoria or in Brixton.
- b. \rightarrow Mr. X might be in Victoria and he might be in Brixton.

Ignorance

- (4) The prize is in the attic or in the garden \sim speaker doesn't know where
- (5) ? I have two or three children.
 - In the standard approach, ignorance inferences are conversational implicatures
 - Less consensus on FC inferences analysed as conversational implicatures; grammatical scalar implicatures; semantic entailments; ...

[Kamp 1973]

[Grice 1989]

[Zimmermann 2000]

- ▶ FC and ignorance inferences are
 - Not the result of Gricean reasoning
 - Not the effect of applications of covert grammatical operators

```
\neq scalar implicatures]
```

 \neq semantic entailments

 \neq conversational implicatures

 But rather a consequence of something else speakers do in conversation, namely,

NEGLECT-ZERO

when interpreting a sentence speakers create structures representing reality¹ and in doing so they systematically neglect structures which verify the sentence by virtue of an empty configuration (*zero-models*)

Tendency to neglect zero-models follows from the difficulty of the cognitive operation of evaluating truths with respect to empty witness sets [Nieder 2016, Bott et al, 2019]

¹Johnson-Laird (1983) Mental Models. Cambridge University Press.

Illustrations

- (6) Every square is black.
 - a. Verifier: $[\blacksquare, \blacksquare, \blacksquare]$
 - b. Falsifier: $[\blacksquare, \Box, \blacksquare]$
 - c. Zero-models: []; $[\triangle, \triangle, \triangle]$; $[\diamond, \blacktriangle, \diamond]$; $[\blacktriangle, \blacktriangle, \blacktriangle]$; ...
- (7) Less than three squares are black.
 - a. Verifier: $[\blacksquare, \Box, \blacksquare]$
 - b. Falsifier: [■, ■, ■]
 - c. Zero-models: []; $[\Box, \Box, \Box]$; $[\triangle, \triangle, \triangle]$; $[\diamond, \blacktriangle, \diamond]$; $[\blacktriangle, \blacktriangle, \blacktriangle]$; ...
 - Cognitive difficulty of zero-models confirmed by experimental findings from number cognition and has been argued to explain
 - the special status of 0 among the natural numbers [Nieder, 2016]
 - why downward-monotonic quantifiers are more costly to process than upward-monotonic ones (*less* vs *more*)
 [Bott et al., 2019]
 - existential import & connexive principles from Aristotle (every A is $B \Rightarrow$ some A is B; not (if A then not A)) [MA & Knudstorp, 2024]

Core idea: tendency to neglect zero-models, assumed to be operative in ordinary conversation, explains FC and related inferences

Illustrations

- (8) It is raining.

 - b. Falsifier: [☆☆☆]
 - c. Zero-models: none
- (9) It is snowing.
 - a. Verifier: [****]
 - b. Falsifier: [^{汝, 汝, ☆}]; [*/// //// ///*];
 - c. Zero-models: none
- (10) It is raining or snowing.

 - b. Falsifier: [☆☆☆]
 - c. Zero-models: [////////]; [*****]
 - Two models in (10-c) are zero-models because they verify the sentence by virtue of an empty witness for one of the disjuncts
 - Ignorance effects arise because such zero-models are cognitively taxing and therefore disregarded in everyday reasoning and conversation

A new conjecture: no-split

A closer look at the disjunctive case

- (11) It is raining or snowing.
 - a. Verifier: [//////// | ****]
 - b. Falsifier: [华华华]
 - c. Zero-models: [/////////]; [♥♥♥♥]
 - ► The "split" verifier in (11-a) involves the entertainment of two alternatives → also a cognitively difficult operation

NO-SPLIT CONJECTURE [Klochowicz, Sbardolini & MA 2024] the ability to split states (entertain multiple alternatives) is acquired late

 \Leftarrow "split" state

- The combination of neglect-zero & no-split can explain non-classical inferences observed in pre-school children [Singh et al 2016]
 - (12) The boy is holding an apple or a banana = The boy is holding an apple and a banana $(\alpha \lor \beta) \equiv (\alpha \land \beta)$
 - (13) The boy is not holding an apple or a banana = The boy is neither holding an apple nor a banana $\neg(\alpha \lor \beta) \equiv \neg \alpha \land \neg \beta$
 - (14) Every boy is holding an apple or a banana = Every boy is holding an apple and a banana $\forall x(\alpha \lor \beta) \equiv \forall x(\alpha \land \beta)$

BSML: teams and bilateralism

Team semantics: formulas interpreted wrt a set of points of evaluation (a team) rather than single ones [Hodges 1997; Väänänen 2007]

Classical vs team-based modal logic

Classical modal logic:

```
M, w \models \phi, where w \in W
```

Team-based modal logic:

```
M, t \models \phi, where t \subseteq W
```

Bilateral state-based modal logic (BSML)

- Teams \mapsto information states [Dekker93; Groenendijk⁺96; Ciardelli⁺19]
- Assertion & rejection conditions modelled rather than truth

- Neglect-zero tendency modelled by NE
- BSML^F: No-split modelled via a flattening operator F

[Yang & Väänänen 2017]

 $[M = \langle W, R, V \rangle]$ (truth in worlds)

BSML: Classical Modal Logic + NE

Language

$$\phi := \mathbf{p} \mid \neg \phi \mid \phi \lor \phi \mid \phi \land \phi \mid \diamond \phi \mid \text{NE}$$

Bilateral team semantics

Given a Kripke model $M = \langle W, R, V \rangle$ & states $s, t, t' \subseteq W$

Validity: $\phi_1, \ldots, \phi_n \models \psi$ iff for all M, s: $M, s \models \phi_1, \ldots, M, s \models \phi_n \Rightarrow M, s \models \psi$ Proof Theory: See Anttila 2021; Anttila et al. 2024.



Team-sensitive constraints on accessibility relation

- R is indisputable in (M, s) iff ∀w, v ∈ s : R[w] = R[v] → all worlds in s access exactly the same set of worlds
- ▶ *R* is state-based in (M, s) iff $\forall w \in s : R[w] = s$ \mapsto all and only worlds in *s* are accessible within *s*



(a) indisputable



(b) state-base (& indisputable)



(c) neither

Deontic vs epistemic modals

- Difference deontic vs epistemic modals captured by different properties of accessibility relation:
 - Epistemics: *R* is state-based
 - Deontics: R is possibly indisputable

(e.g. in performative uses)

Neglect-zero effects in BSML: split disjunction

A state s supports a disjunction (φ ∨ ψ) iff s is the union of two substates, each supporting one of the disjuncts



Figure: Models for $(a \lor b)$.

- ► { w_a } verifies ($a \lor b$) by virtue of an empty witness for the second disjunct, { w_a } = { w_a } $\cup \emptyset \& M, \emptyset \models b$ [\mapsto zero-model]
- Main idea: define neglect-zero enrichments, []⁺, whose core effect is to rule out such zero-models
- Implementation: []⁺ defined using NE (s ⊨ NE iff s ≠ Ø), which models neglect-zero in the logic

BSML: neglect-zero enrichment

Non-emptiness

 $\ensuremath{\operatorname{NE}}$ is supported in a state if and only if the state is not empty

$$M, s \models \text{NE} \quad \text{iff} \quad s \neq \emptyset$$
$$M, s \models \text{NE} \quad \text{iff} \quad s = \emptyset$$

Neglect-zero enrichment

For NE-free α , $[\alpha]^+$ defined as follows:

$$[p]^+ = p \land \text{NE}$$

$$[\neg \alpha]^+ = \neg [\alpha]^+ \land \text{NE}$$

$$[\alpha \lor \beta]^+ = ([\alpha]^+ \lor [\beta]^+) \land \text{NE}$$

$$[\alpha \land \beta]^+ = ([\alpha]^+ \land [\beta]^+) \land \text{NE}$$

$$[\Diamond \alpha]^+ = \Diamond [\alpha]^+ \land \text{NE}$$

[]+ enriches formulas with the requirement to satisfy $\ensuremath{\operatorname{NE}}$ distributed along each of their subformulas

Neglect-zero effects in BSML: enriched disjunction

s supports an enriched disjunction [φ ∨ ψ]⁺ iff s is the union of two non-empty substates, each supporting one of the disjuncts



An enriched disjunction requires both disjuncts to be live possibilities

- (15) It is raining or snowing \sim It might be raining and it might be snowing $[\alpha \lor \beta]^+ \models \diamondsuit_e \alpha \land \diamondsuit_e \beta$ (where *R* is state-based)
- Main result: in BSML []⁺-enrichment has non-trivial effect only when applied to *positive* disjunctions²
 - \mapsto we derive FC and related effects (for enriched formulas);
 - \mapsto []⁺-enrichment vacuous under single negation.

²MA (2022) Logic and Conversation: the case of free choice. Semantics and Pragmatics 15(5).

Zero and no-zero models

(M, s) is a zero-model for α iff $M, s \models \alpha$, but $M, s \not\models [\alpha]^+$ (M, s) is a no-zero verifier for α iff $M, s \models [\alpha]^+$

More no-zero verifiers for enriched disjunction



Neglect-zero and no-split

▶ More no-zero verifiers for *a* ∨ *b*:



 $\left\{ w_{ab} \right\}$ is a no-split verifier for the disjunction: no alternatives entertained;

- No-split conjecture: only no-split verifiers accessible to 'conjunctive' pre-school children [Klochowicz, Sbardolini, MA, 2024]
- Implementation: uses flattening operator F

 $M, s \models F\phi$ iff for all $w \in s : M, \{w\} \models \phi$

 $\mathsf{Flattening} \mapsto \mathsf{formulas} \ \mathsf{always} \ \mathsf{interpreted} \ \mathsf{wrt} \ \mathsf{to} \ \mathsf{singleton} \ \mathsf{substates}$

Combination of no-split and no-zero yields conjunctive or:

$$[\mathbf{F}(\alpha \lor \beta)]^+ \equiv \alpha \land \beta$$
$$[\neg \mathbf{F}(\alpha \lor \beta)]^+ \equiv \neg \alpha \land \neg \beta$$

Illustration: combination of no-split and no-zero yields conjunctive or



Figure: Models for $(a \lor b)$



[α ∨ β]⁺ ⊨ ◊_eα ∧ ◊_eβ; ⊭ α ∧ β [adult-like]
F(α ∨ β) ⊭ ◊_eα ∧ ◊_eβ; ⊭ α ∧ β [logician]
[F(α ∨ β)]⁺ ⊨ α ∧ β ['conjunctive' children]

Neglect-zero effects in BSML: possibility vs uncertainty

More no-zero verifiers for a ∨ b:



Two components of full ignorance ('speaker doesn't know which'):³

- (17) It is raining or it is snowing $(\alpha \lor \beta) \rightsquigarrow$
 - a. Uncertainty: $\neg \Box_e \alpha \land \neg \Box_e \beta$
 - b. Possibility: $\diamond_e \alpha \land \diamond_e \beta$ (equiv $\neg \Box_e \neg \alpha \land \neg \Box_e \neg \beta$)
- Fact: Only possibility derived as neglect-zero effect:

►
$$[a \lor b]^+ \models \Diamond_e a \land \Diamond_e b$$
 (if *R* is state-based)
► $\{w_{ab}, w_a\} \models [a \lor b]^+$, but $\nvDash \neg \square_e a$

• $\{w_{ab}\} \models [a \lor b]^+$, but $\not\models \neg \Box_e a; \not\models \neg \Box_e b$

³Degano, Marty, Ramotowska, MA, Breheny, Romoli, Sudo. SuB & XPRAG, 2023.

Two derivations of full ignorance

1. Standard neo-Gricean derivation [Sauerland 2004] (i) Uncertainty derived through quantity reasoning (18) $\alpha \lor \beta$ ASSERTION (19) $\neg \Box_e \alpha \wedge \neg \Box_e \beta$ UNCERTAINTY (from QUANTITY) (ii) Possibility derived from uncertainty and quality about assertion (20) $\Box_e(\alpha \lor \beta)$ QUALITY ABOUT ASSERTION (21) $\Rightarrow \diamond_e \alpha \land \diamond_e \beta$ POSSIBILITY 2. Neglect-zero derivation (i) Possibility derived as neglect-zero effect (22) $\alpha \lor \beta$ ASSERTION (23) $\Diamond_e \alpha \land \Diamond_e \beta$ POSSIBILITY (from NEGLECT-ZERO) (ii) Uncertainty derived from possibility and scalar reasoning (24) $\neg(\alpha \land \beta)$ SCALAR IMPLICATURE (25) $\Rightarrow \neg \Box_e \alpha \land \neg \Box_e \beta$ UNCERTAINTY

Contrasting predictions of competing accounts of ignorance

- Neo-Gricean: No possibility without uncertainty
- Neglect-zero: Possibility derived independently from uncertainty

Experimental findings

- Using adapted mystery box paradigm, compared conditions in which
 - both uncertainty and possibility are false
 - uncertainty false but possibility true [no-zero, no-uncertain model]
- Less acceptance when possibility is false (95% vs 44%)
- \Rightarrow Evidence that possibility can arise without uncertainty
- A challenge for the traditional neo-gricean approach



Figure: Models for $(a \lor b)$

[Degano et al 2023]

[zero-model]

| | NS FC | Dual Prohib | Universal FC | Double Neg | WS FC |
|--------------|-------|-------------|--------------|------------|-------|
| Neo-Gricean | yes | yes | no | ? | no |
| Grammatical | yes | yes* | yes | no* | no* |
| Semantic | yes | no* | yes | no* | no |
| Neglect-zero | yes | yes | yes | yes | yes |

Comparison with competing accounts of $\ensuremath{\operatorname{FC}}$ inference

Argument in favor of neglect-zero hypothesis

Empirical coverage: FC sentences give rise to a complex pattern of inferences

- Captured by neglect-zero approach implemented in BSML⁴
- Most other approaches need additional assumptions

⁴MA (2022). Logic and conversation: the case of FC. Sem & Pra, 15(5).

The data

(27)**Dual Prohibition** [Alonso-Ovalle 2006, Marty et al. 2021]

You are not allowed to eat the cake or the ice-cream а \sim You are not allowed to eat either one.

b.
$$\neg \diamondsuit(\alpha \lor \beta) \rightsquigarrow \neg \diamondsuit \alpha \land \neg \diamondsuit \beta$$

(28)Universal FC [Chemla 2009]

All of the boys may go to the beach or to the cinema. а \sim All of the boys may go to the beach and all of the boys may go to the cinema

b.
$$\forall x \diamondsuit (\alpha \lor \beta) \rightsquigarrow \forall x (\diamondsuit \alpha \land \diamondsuit \beta)$$

(29)Double Negation FC [Gotzner et al. 2020]

- Exactly one girl cannot take Spanish or Calculus. а \sim One girl can take neither of the two and each of the others can choose between them
- b $\exists x (\neg \Diamond (\alpha(x) \lor \beta(x)) \land \forall y (y \neq x \to \neg \neg \Diamond (\alpha(y) \lor \beta(y)))) \rightsquigarrow$ $\exists x (\neg \Diamond \alpha(x) \land \neg \Diamond \beta(x) \land \forall y (y \neq x \to (\Diamond \alpha(y) \land \Diamond \beta(y))))$
- (30)Wide Scope FC

[Zimmermann 2000, Hoeks et al. 2017]

- а Detectives may go by bus or they may go by boat. \sim Detectives may go by bus and may go by boat.
- Mr. X might be in Victoria or he might be in Brixton. b \sim Mr. X might be in Victoria and might be in Brixton.
- c. $\Diamond \alpha \lor \Diamond \beta \rightsquigarrow \Diamond \alpha \land \Diamond \beta$

Neglect-zero effects in BSML: FC predictions

After enrichment

We derive both wide and narrow scope FC inferences:

- Narrow scope FC: $[\Diamond(\alpha \lor \beta)]^+ \models \Diamond \alpha \land \Diamond \beta$
- ▶ Universal FC: $[\forall x \diamond (\alpha \lor \beta)]^+ \models \forall x (\diamond \alpha \land \diamond \beta)$ ▶ Double negation FC: $[\neg \neg \diamond (\alpha \lor \beta)]^+ \models \diamond \alpha \land \diamond \beta$
- Wide scope FC: $[\Diamond \alpha \lor \Diamond \beta]^+ \models \Diamond \alpha \land \Diamond \beta$

(if *R* is indisputable)

- while no undesirable side effects obtain with other configurations:
 - **Dual prohibition:** $[\neg \Diamond (\alpha \lor \beta)]^+ \models \neg \Diamond \alpha \land \neg \Diamond \beta$

Before enrichment

The NE-free fragment of BSML is equivalent to classical modal logic:

$$\alpha \models_{BSML^{\emptyset}} \beta \text{ iff } \alpha \models_{CML} \beta \qquad [\alpha, \beta \text{ are NE-free}]$$

- But we can capture the infelicity of epistemic contradictions [Yalcin, 2007] by putting team-based constraints on the accessibility relation:
 - (if R is state-based) **1**. Epistemic contradiction: $\Diamond \alpha \land \neg \alpha \models \bot$
 - 2. Non-factivity: $\Diamond \alpha \not\models \alpha$

BSML & related systems: information states vs possible worlds

Failure of bivalence in BSML

 $M, s \not\models p \& M, s \not\models \neg p$, for some info state s

- Info states: less determinate than possible worlds
 - just like truthmakers, situations, possibilities, ...
- Technically:
 - Truthmakers/possibilities: points in a partially ordered set
 - Info states: sets of possible worlds, also elements of a partially ordered set, the Boolean lattice Pow(W)
- Thus systems using these structures are closely connected, although might diverge in motivation:
 - Truthmaker & possibility semantics: description of ontological structures in the world
 - BSML: explaining patterns in inferential & communicative human activities
- ► Next:
 - Comparison via translations in Modal Information Logic [vBenthem19]

BSML & related systems: comparisons via translation

- Modal Information Logic (MIL) (van Benthem, 1989, 2019):⁵ common ground where related systems can be interpreted and their connections and differences can be explored
- Next: (simplified) translations into MIL of the following systems:
 - BSML
 - Truthmaker semantics (Fine)
 - Possibility semantics (Humberstone, Holliday)
 - Inquisitive semantics (Ciardelli, Groenendijk & Roelofsen)
 - (cf. Gödel's (1933) translation of intuitionistic logic into modal logic)
- Focus on propositional fragments
 - disjunction
 - negation
- (Based on work in progress with Søren B. Knudstorp, Nick Bezhanishvili, Johan van Benthem and Alexandru Baltag)

⁵Johan van Benthem (2019) Implicit and Explicit Stances in Logic, *Journal of Philosophical Logic*.

Modal Information Logic (MIL)

Language

$$\phi \quad ::= \quad p \mid \neg \phi \mid \phi \land \phi \mid \phi \lor \phi \mid \langle sup \rangle \phi \psi$$

where $p \in A$.

Models and interpretation

Formulas are interpreted on triples $M = (X, \leq, V)$ where \leq is a partial order

$$\begin{array}{lll} \mathcal{M}, x \models \rho & \text{iff} & x \in V(p) \\ \mathcal{M}, x \models \neg \phi & \text{iff} & \mathcal{M}, x \not\models \phi \\ \mathcal{M}, x \models \phi \land \psi & \text{iff} & \mathcal{M}, x \models \phi \text{ and } \mathcal{M}, x \models \psi \\ \mathcal{M}, x \models \phi \lor \psi & \text{iff} & \mathcal{M}, x \models \phi \text{ or } \mathcal{M}, x \models \psi \\ \mathcal{M}, x \models \langle sup \rangle \phi \psi & \text{iff} & \text{there are } y, z : x = sup_{\leq}(y, z) \& \mathcal{M}, y \models \phi \& \mathcal{M}, z \models \psi \\ \vec{x} \leq]\phi = \neg \langle sup \rangle (\neg \varphi) \top \\ \mathcal{M}, x \models [\leq]\phi & \text{iff} & \text{for all } y : y \leq x \Rightarrow \mathcal{M}, y \models \phi \end{array}$$

Modal Information Logic (MIL)



Translations into Modal Information Logic

BSML (non-modal NE-free fragment): \leq is subset relation \subseteq

$$(\neg \phi)^+ = (\phi)^-$$

$$(\neg \phi)^- = (\phi)^+$$

$$(\phi \lor \psi)^+ = \langle sup \rangle (\phi)^+ (\psi)^+$$

$$(\phi \lor \psi)^- = (\phi)^- \land (\psi)^-$$

$$(\phi \land \psi)^+ = (\phi)^+ \land (\psi)^+$$

$$(\phi \land \psi)^- = \langle sup \rangle (\phi)^- (\psi)^-$$

. . .

. . .

Furthmaker semantics (Fine): \leq is "part of" relation

$$(\neg \phi)^+ = (\phi)^- (\neg \phi)^- = (\phi)^+ (\phi \lor \psi)^+ = (\phi)^+ \lor (\psi)^+ (\phi \lor \psi)^- = \langle sup \rangle (\phi)^- (\psi)^- (\phi \land \psi)^+ = \langle sup \rangle (\phi)^+ (\psi)^+ (\phi \land \psi)^- = (\phi)^- \lor (\psi)^-$$

Translations into Modal Information Logic

Possibility semantics (Humberstone, Holliday)

$$\begin{array}{lll} tr(\neg\phi) &=& [\leq]\neg tr(\phi) \\ tr(\phi \land \psi) &=& tr(\phi) \land tr(\psi) \\ tr(\phi \lor \psi) &=& [\leq] \langle \leq \rangle (tr(\phi) \lor tr(\psi)) \\ & & \cdot \end{array}$$

Inquisitive semantics (Groenendijk, Roelofsen and Ciardelli)

.

$$\begin{array}{l} \vdots \\ tr(\neg\phi) &= [\leq]\neg tr(\phi) \\ tr(\phi \land \psi) &= tr(\phi) \land tr(\psi) \\ tr(\phi \lor \psi) &= tr(\phi) \lor tr(\psi) \end{array}$$

Disjunction and Negation

- Three notions of disjunction expressible in MIL:
 - ▶ Boolean disjunction: $\phi \lor \psi$ [classical logic, intuitionistic logic, inquisitive logic]
 - Lifted/split disjunction: $\langle sup \rangle \phi \psi$ [BSML, dependence logic, team semantics]
 - Cofinal disjunction: [co](φ ∨ ψ) [possibility semantics, dynamic semantics]
- Three notions of negation:
 - Boolean negation: ¬φ [classical logic, ...]
 - ▶ Bilateral negation: $(\neg \phi)^+ = (\phi)^- \& (\neg \phi)^- = (\phi)^+$ [truthmaker semantics, BSML, ...]
 - Intuitionistic-like negation: [≤]¬φ [possibility semantics, inquisitive semantics, intuitionistic logic]

Some combinations:

- ▶ Boolean disjunction + boolean negation \mapsto classical logic
- Boolean notions in other combinations can generate non-classicality:
 - ▶ Boolean disjunction + intuitionistic negation → intuitionistic logic
- Classicality also generated by non-boolean combinations:
 - Split disjunction + bilateral negation (classical fragm. BSML)

(where $[co]\phi =: [\leq] \langle \leq \rangle \phi$)

Conclusions

- ▶ FC and ignorance: a mismatch between logic and language
- Grice's insight:
 - stronger meanings can be derived paying more "attention to the nature and importance to the conditions governing conversation"
- Nihil proposal: non-classical inferences consequences of cognitive biases
 - FC and ignorance as neglect-zero effects

Literal meanings (NE-free fragment) + cognitive factors (NE) \Rightarrow FC & possibility inferences

Conjunctive or as no-zero + no-split effect

Literal meanings (NE-free fragment) + cognitive factors (NE, F) \Rightarrow conjunctive or

- ▶ Implementation in BSML^F (a team-based modal logic)
- Differences but also interesting connections with related systems
- MIL useful framework for comparisons via translations

Collaborators & related (future) research

Logic

Proof theory (<u>Anttila, Yang</u>); expressive completeness (<u>Anttila, Knudstorp</u>); bimodal perspective (<u>Knudstorp, Baltag, van</u> <u>Benthem, Bezhanishvili</u>); qBSML (<u>van Ormondt</u>); BiUS & qBiUS (<u>MA</u>); typed BSML (<u>Muskens</u>); connexive logic (Knudstorp & MA);...

Language

FC cancellations (<u>Pinton, Hui</u>); modified numerals (<u>vOrmondt</u>); attitude verbs (<u>Yan</u>); conditionals (<u>Flachs</u>); questions (<u>Klochowicz</u>); quantifiers (<u>Klochowicz</u>, Bott, <u>Schlotterbeck</u>); indefinites (<u>Degano</u>); homogeneity (<u>Sbardolini</u>); acquisition (<u>Klochowicz</u>, <u>Sbardolini</u>); experiments (<u>Degano</u>, Klochowicz, Ramotowska, Bott, <u>Schlotterbeck</u>, <u>Marty, Breheny, Romoli, Sudo</u>); ...

Thank You!⁶

⁶This work was supported by NWO OC project Nothing is Logical (grant no 406.21.CTW.023).